

1. Let F_n denote the n th Fibonacci number. Show that $F_n = 5F_{n-4} + 3F_{n-5}$ whenever $n > 5$. Use this result to show that F_n is divisible by 5 whenever n is divisible by 5.

Your answer here...

2. We say that a is relatively prime to b if $(a, b) = 1$.

- (a) *Find all positive integers less than 10 that are relatively prime to 10.*

Your answer here...

- (b) *Find all positive integers less than 11 that are relatively prime to 11.*

Your answer here...

3. Are there integers a, b , and c so that $a \mid bc$ but $a \nmid b$ and $a \nmid c$?

Your answer here...

4. (a) *Show that if $a \in \mathbb{Z}$, then $3 \mid a^3 - a$*

Your answer here...

- (b) *Show that if $a \in \mathbb{Z}$, then $5 \mid a^5 - a$*

Your answer here...