

1. *Let  $F_n$  denote the  $n$ th Fibonacci number. Show that  $F_n = 5F_{n-4} + 3F_{n-5}$  whenever  $n > 5$ . Use this result to show that  $F_n$  is divisible by 5 whenever  $n$  is divisible by 5.*

Your answer here...

2. We say that  $a$  is relatively prime to  $b$  if  $(a, b) = 1$ .

- (a) *Find all positive integers less than 10 that are relatively prime to 10.*

Your answer here...

- (b) *Find all positive integers less than 11 that are relatively prime to 11.*

Your answer here...

3. Are there integers  $a, b$ , and  $c$  so that  $a \mid bc$  but  $a \nmid b$  and  $a \nmid c$ ?

Your answer here...

4. (a) *Show that if  $a \in \mathbb{Z}$ , then  $3 \mid a^3 - a$*

Your answer here...

- (b) *Show that if  $a \in \mathbb{Z}$ , then  $5 \mid a^5 - a$*

Your answer here...