

KEY

# 1.5 Recommended Exercises

1-5, 11-15, 21-~~25~~ 31

- 2) 1.  $p \rightarrow (\sim q)$   
 2.  $\sim p$   
 $\therefore q$

- 4) 1.  $p \rightarrow (\sim q)$   
 2.  $\sim q$   
 $\therefore p$

12) We want to check  $[(p \rightarrow (\sim q)) \wedge (\sim p)] \rightarrow q$

P	q	② $\sim p$	$\sim q$	① $p \rightarrow (\sim q)$	① $\wedge$ ②	(① $\wedge$ ②) $\rightarrow q$
T	T	F	F	F	F	T
T	F	F	T	T	F	T
F	T	T	F	T	T	T
F	F	T	T	T	T	F

The argument is invalid

The instance which causes the argument to be invalid is when p and q are both false (this is called a counterexample — but you don't need to know this for the test)

4) We want to check  $[(p \rightarrow (\sim q)) \wedge (\sim q)] \rightarrow p$

P	q	② $\sim q$	① $p \rightarrow (\sim q)$	① $\wedge$ ②	[① $\wedge$ ②] $\rightarrow p$
T	T	F	F	F	T
T	F	T	T	T	T
F	T	F	T	F	T
F	F	T	T	T	F

The argument is invalid.

The counterexample is when p and q are both false

22)  $t$ : you watch television  
 $b$ : you read books  
 $w$ : you are wise

Argument: 1.  $t \rightarrow (\sim b)$   
 2.  $b \rightarrow w$   
 $\therefore t \rightarrow (\sim w)$

We care about the sentence  $[(1) \wedge (2)] \rightarrow \therefore$

Truth table

$t$	$b$	$w$	<del><math>(\sim b)</math></del>	① $t \rightarrow (\sim b)$	② $b \rightarrow w$	$\sim w$	③ $t \rightarrow (\sim w)$	① $\wedge$ ②	(① $\wedge$ ②) $\rightarrow$ ③
T	T	T	F	F	T	F	F	F	T
T	T	F	F	F	F	T	T	F	T
T	F	T	T	T	T	F	F	T	T
T	F	F	T	T	T	T	T	T	F
F	T	T	F	T	T	F	T	T	T
F	T	F	F	T	F	T	T	F	T
F	F	T	T	T	T	F	T	T	T
F	F	F	T	T	T	T	T	T	T

The argument is invalid, with the counterexample being when  $t$  and  $w$  are true, with  $b$  being false.

24) See Ex 4a on Lecture Guide 1.5

26)  $h$ : you can afford health insurance  
 $u$ : you are unemployed  
 $p$ : you are a politician  
 Argument: 1.  $h \rightarrow (\sim u)$   
 2.  $p \rightarrow h$   
 $\therefore p \rightarrow (\sim u)$

We care about  $[(1) \wedge (2)] \rightarrow \therefore$

Truth table

$p$	$h$	$u$	$\sim u$	① $h \rightarrow (\sim u)$	② $p \rightarrow h$	① $\wedge$ ②	③ $p \rightarrow (\sim u)$	(① $\wedge$ ②) $\rightarrow$ ③
T	T	T	F	F	T	F	F	T
T	T	F	T	T	T	T	T	T
T	F	T	F	T	F	F	F	T
T	F	F	T	T	T	T	T	T
F	T	T	F	F	T	F	T	T
F	T	F	T	T	T	T	T	T
F	F	T	F	T	F	F	F	T
F	F	F	T	T	T	T	T	T

Therefore, the argument is valid

28) See Ex 4b on Lecture Guide 1.5

30)  $a$ : someone is an artist  
 $l$ : someone is a lawyer  
 $m$ : someone is a musician

Argument: 1.  $a \rightarrow (\sim l)$   
 2.  $l \rightarrow (\sim m)$   
 $\therefore a \rightarrow (\sim m)$

We care about  $[(1) \wedge (2)] \rightarrow \therefore$

$a$	$l$	$m$	$\sim l$	$\sim m$	$a \rightarrow (\sim l)$ <sup>(1)</sup>	$l \rightarrow (\sim m)$ <sup>(2)</sup>	$a \rightarrow (\sim m)$ <sup>(3)</sup>	$(1) \wedge (2)$	$((1) \wedge (2)) \rightarrow (3)$
T	T	T	F	F	F	F	F	F	T
T	T	F	F	T	F	T	T	F	T
T	F	T	T	F	T	T	F	T	F
T	F	F	T	T	T	T	T	T	T
F	T	T	F	F	T	F	T	F	T
F	T	F	F	T	T	T	T	T	T
F	F	T	T	F	T	T	T	T	T
F	F	F	T	T	T	T	T	T	T

The argument is invalid, with the counterexample being when ~~an~~  $a$  and  $m$  are true, but  $l$  is false

